

Arizona Mathematics Standards	Boardworks Middle School Math Presentations
Grade 6	
Strand 1: Number and Operations, Concept 1: Number Sense	
PO 1. Convert between expressions for positive rational numbers, including fractions, decimals, percents, and ratios.	Equivalent fractions, decimals and percentages Equivalent fractions Fractions and decimals Introducing percentages Ratio and rate
PO 2. Use prime factorization to <ul style="list-style-type: none"> • express a whole number as a product of its prime factors and • determine the greatest common factor and least common multiple of two whole numbers. 	Prime factorization GCF and LCM
PO 3. Demonstrate an understanding of fractions as rates, division of whole numbers, parts of a whole, parts of a set, and locations on a real number line.	Fractions of shapes Ordering fractions Finding a fraction of an amount Ratio and rate Dividing in a given ratio Ratio and proportion problems
PO 4. Compare and order integers; and positive fractions, decimals, and percents.	Ordering integers Ordering fractions Ordering decimals Introducing percentages Equivalent fractions, decimals and percentages Using negative numbers in context
PO 5. Express that a number's distance from zero on the number line is its absolute value.	Absolute value
PO 6. Express the inverse relationships between exponents and roots for perfect squares and cubes.	Square roots Cubes and cube roots

Strand 1: Number and Operations, Concept 2: Numerical Operations	
PO 1. Apply and interpret the concepts of addition and subtraction with integers using models.	Adding and subtracting integers Adding and subtracting integers activities
PO 2. Multiply multi-digit decimals through thousandths.	Multiplying and dividing by 0.1 and 0.01 Multiplying by numbers between 0 and 1 Mental math and place value Mental math puzzles Mental multiplication
PO 3. Divide multi-digit whole numbers and decimals by decimal divisors with and without remainders.	Mental math puzzles Multiplying and dividing by 0.1 and 0.01 Mental division
PO 4. Multiply and divide fractions.	Multiplying fractions Dividing by fractions
PO 5. Provide a mathematical argument to explain operations with two or more fractions or decimals.	Adding and subtracting simple fractions Methods for adding and subtracting fractions Multiplying and dividing by 0.1 and 0.01 Multiplying by numbers between 0 and 1
PO 6. Apply the commutative, associative, distributive, and identity properties to evaluate numerical expressions involving whole numbers.	Properties of numbers
PO 7. Simplify numerical expressions (involving fractions, decimals, and exponents) using the order of operations with or without grouping symbols.	Order of operations and PEMDAS
Strand 1: Number and Operations, Concept 3: Estimation	
PO 1. Use benchmarks as meaningful points of comparison for rational numbers.	-
PO 2. Make estimates appropriate to a given situation and verify the reasonableness of the results.	Estimation and approximation Checking results
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 1: Data Analysis (Statistics)	
PO 1. Solve problems by selecting, constructing, and interpreting displays of data, including histograms and stem-and-leaf plots.	Appropriate graphs Histograms Calculating statistics Bar graphs Line graphs Circle graphs Collecting data

PO 2. Formulate and answer questions by interpreting, analyzing, and drawing inferences from displays of data, including histograms and stem-and-leaf plots.	Appropriate graphs Histograms Calculating statistics Line graphs Circle graphs Bar graphs
PO 3. Use extreme values, mean, median, mode, and range to analyze and describe the distribution of a given data set.	Finding the mode Finding the median Finding the range Calculating statistics Calculating the mean Comparing data
PO 4. Compare two or more sets of data by identifying trends.	Comparing data
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 2: Probability	
PO 1. Use data collected from multiple trials of a single event to form a conjecture about the theoretical probability.	Experimental probability
PO 2. Use theoretical probability to •predict experimental outcomes, •compare the outcome of the experiment to the prediction, and •replicate the experiment and compare results.	Probability diagrams The language of probability Calculating probability part 1 Experimental probability
PO 3. Determine all possible outcomes (sample space) of a given situation using a systematic approach.	Probability diagrams
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 3: Systematic Listing and Counting	
PO 1. Build and explore tree diagrams where items repeat.	-
PO 2. Explore counting problems with Venn diagrams using three attributes.	Venn diagrams
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 4: Vertex-Edge Graphs	
PO 1. Investigate properties of vertex-edge graphs •Hamilton paths, •Hamilton circuits, and •shortest route.	-
PO 2. Solve problems related to Hamilton paths and circuits.	-

Strand 3: Patterns, Algebra, and Functions, Concept 1: Patterns	
PO 1. Recognize, describe, create, and analyze a numerical sequence involving fractions and decimals using all four basic operations.	<ul style="list-style-type: none"> Introducing sequences Sequences from geometrical patterns Describing and continuing sequences Generating sequences from flow charts Generating sequences and rules
Strand 3: Patterns, Algebra, and Functions, Concept 2: Functions and Relationships	
PO 1. Recognize and describe a relationship between two quantities, given by a chart, table, or graph, using words and expressions.	<ul style="list-style-type: none"> Direct variations Function machines Mapping functions Graphs of functions The equation of a straight line
Strand 3: Patterns, Algebra, and Functions, Concept 3: Algebraic Representations	
PO 1. Use an algebraic expression to represent a quantity in a given context.	<ul style="list-style-type: none"> Writing expressions Introducing formulas
PO 2. Create and solve two-step equations that can be solved using inverse properties with fractions and decimals.	<ul style="list-style-type: none"> Solving simple equations Substitution Dividing algebraic terms Multiplying algebraic terms Combining like terms
PO 3. Translate both ways between a verbal description and an algebraic expression or equation.	<ul style="list-style-type: none"> Writing expressions
PO 4. Evaluate an expression involving the four basic operations by substituting given fractions and decimals for the variable.	<ul style="list-style-type: none"> Substitution

Strand 3: Patterns, Algebra, and Functions, Concept 4: Analysis of Change	
PO 1. Determine a pattern to predict missing values on a line graph or scatterplot.	Direct variations Conversion graphs Graphs of functions
Strand 4: Geometry and Measurement, Concept 1: Geometric Properties	
PO 1. Define π (pi) as the ratio between the circumference and diameter of a circle and explain the relationship among the diameter, radius, and circumference.	Circles Circumference of a circle
PO 2. Solve problems using properties of supplementary, complementary, and vertical angles.	Calculating angles Angles in polygons
Strand 4: Geometry and Measurement, Concept 2: Transformation of Shapes	
PO 1. Identify a simple translation or reflection and model its effect on a 2-dimensional figure on a coordinate plane using all four quadrants.	Translation Reflection
PO 2. Draw a reflection of a polygon in the coordinate plane using a horizontal or vertical line of reflection.	Reflection
Strand 4: Geometry and Measurement, Concept 3: Coordinate Geometry	
PO 1. Graph ordered pairs in any quadrant of the coordinate plane.	Introducing coordinates Reading and plotting graphs
PO 2. State the missing coordinate of a given figure on the coordinate plane using geometric properties to justify the solution.	Quadrilaterals on a coordinate grid
Strand 4: Geometry and Measurement, Concept 4: Measurement	
PO 1. Determine the appropriate unit of measure for a given context and the appropriate tool to measure to the needed precision (including length, capacity, angles, time, and mass).	Measuring angles Customary unit conversions Converting metric units Estimating measurements
PO 2. Solve problems involving conversion within the U.S. Customary and within the metric system.	Customary unit conversions Converting metric units
PO 3. Estimate the measure of objects using a scale drawing or map.	Scale drawings
PO 4. Solve problems involving the area of simple polygons using formulas for rectangles and triangles.	Area Using formulas
PO 5. Solve problems involving area and perimeter of regular and irregular polygons.	Area Area of irregular shapes Area problems Perimeter
PO 6. Describe the relationship between the volume of a figure and the area of its base.	Cylinders, cones and spheres Volume

Grade 7	
Strand 1: Number and Operations, Concept 1: Number Sense	
PO 1. Recognize and convert between expressions for positive and negative rational numbers, including fractions, decimals, percents, and ratios.	Fractions and decimals Equivalent fractions Equivalent fractions, decimals and percentages Ratio and rate
PO 2. Find or use factors, multiples, or prime factorization within a set of numbers.	Multiples and factors Prime factorization
PO 3. Compare and order rational numbers using various models and representations.	Ordering integers Ordering decimals Ordering fractions Using negative numbers in context Inequalities Introducing coordinates
PO 4. Model and solve simple problems involving absolute value.	Absolute value
Strand 1: Number and Operations, Concept 2: Numerical Operations	
PO 1. Add, subtract, multiply, and divide integers.	Adding and subtracting integers Adding and subtracting integers activities Using negative numbers in context Multiplying and dividing integers Divisibility Mental addition and subtraction Mental multiplication Mental division Written methods for addition and subtraction Written methods for multiplication Written methods for division

<p>PO 2. Solve problems with rational numbers and appropriate operations using exact answers or estimates.</p>	<p>Estimation and approximation Adding and subtracting integers Adding and subtracting integers activities Using negative numbers in context Multiplying and dividing integers Divisibility Mental addition and subtraction Mental multiplication Mental division Written methods for addition and subtraction Written methods for multiplication Written methods for division Adding and subtracting simple fractions Methods for adding and subtracting fractions One number as a fraction of another Multiplying fractions Dividing by fractions Multiplying and dividing by 0.1 and 0.01 Multiplying by numbers between 0 and 1</p>
<p>PO 3. Solve problems involving percentages, ratio and proportion, including tax, discount, tips, and part/whole relationships.</p>	<p>Calculating percentages mentally Calculating percentages on paper Calculating percentages with a calculator Percentage change Percentages and inverse operations Comparing proportions Ratio and rate Dividing in a given ratio Ratio and proportion problems Using scale factors Direct proportion</p>
<p>PO 4. Represent and interpret numbers using scientific notation (positive exponents only).</p>	<p>Scientific notation</p>
<p>PO 5. Simplify numerical expressions using the order of operations and appropriate mathematical properties.</p>	<p>Order of operations and PEMDAS Properties of numbers</p>
<p>Strand 1: Number and Operations, Concept 3: Estimation</p>	
<p>PO 1. Estimate and apply benchmarks for rational numbers and common irrational numbers.</p>	<p>Circumference of a circle Estimation and approximation</p>

PO 2. Make estimates appropriate to a given situation.	Estimation and approximation Rounding Estimating measurements
PO 3. Estimate square roots of numbers less than 1000 by locating them between two consecutive whole numbers.	Estimation and approximation Square roots
PO 4. Estimate the measure of an object in one system of units given the measure of that object in another system and the approximate conversion factor.	Converting metric units Customary unit conversions
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 1: Data Analysis (Statistics)	
PO 1. Solve problems by selecting, constructing, and interpreting displays of data including multi-line graphs and scatterplots.	Appropriate graphs Line graphs Scatter plots Histograms Calculating statistics Bar graphs Circle graphs Collecting data
PO 2. Interpret trends in a data set, estimate values for missing data, and predict values for points beyond the range of the data set.	Scatter plots
PO 3. Identify outliers and determine their effect on mean, median, mode, and range.	Calculating statistics Finding the median Finding the mode Calculating the mean Finding the range
PO 4. Distinguish between a simple random and non-random sample.	Population and sampling
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 2: Probability	
PO 1. Determine conditional probabilities (experimental) in compound probability experiments.	Experimental probability
PO 2. Experiment with two different events to determine whether the two events are dependent or independent of each other.	-
PO 3. Compare the results of multiple repetitions of the same probability experiment to the theoretical probability.	Experimental probability Calculating probability part 1
PO 4. Compare probabilities to determine fairness in experimental situations.	The language of probability Experimental probability

Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 3: Systematic Listing and Counting	
PO 1. Analyze relationships among the tree diagrams where items repeat and do not repeat; make numerical connections to the multiplication principle of counting.	Probability diagrams
PO 2. Solve counting problems using Venn diagrams and represent the answer algebraically.	Venn diagrams
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 4: Vertex-Edge Graphs	
PO 1. Use vertex-edge graphs and algorithmic thinking to represent and find solutions to practical problems related to Euler/Hamilton paths and circuits.	-
Strand 3: Patterns, Algebra, and Functions, Concept 1: Patterns	
PO 1. Recognize, describe, create, and analyze numerical and geometric sequences using tables or graphs; make conjectures about these sequences.	Introducing sequences Sequences from geometrical patterns Describing and continuing sequences Generating sequences from flow charts Generating sequences and rules Finding the nth term Sequences from practical contexts
Strand 3: Patterns, Algebra, and Functions, Concept 2: Functions and Relationships	
PO 1. Use a table of values to graph an equation or proportional relationship; describe the graph's characteristics.	Graphs of functions Direct variations Reading and plotting graphs
Strand 3: Patterns, Algebra, and Functions, Concept 3: Algebraic Representations	
PO 1. Write a single variable algebraic expression or one-step equation given a contextual situation.	Deriving formulas Writing expressions
PO 2. Evaluate an expression containing one or two variables by substituting numbers for the variables.	Substitution

PO 3. Solve multi-step equations using inverse properties with rational numbers.	Solving simple equations Combining like terms Multiplying algebraic terms Dividing algebraic terms Factoring expressions
PO 4. Translate between graphs and tables that represent a linear equation.	Graphs of functions
PO 5. Create and solve two-step equations that can be solved using inverse operations with rational numbers.	Solving simple equations Combining like terms Multiplying algebraic terms Dividing algebraic terms Factoring expressions
PO 6. Create and solve one-step inequalities with whole numbers.	Integer solutions for inequalities Solving linear inequalities
Strand 3: Patterns, Algebra, and Functions, Concept 4: Analysis of Change	
PO 1. Use graphs and tables to model and analyze change.	Distance-time graphs Interpreting graphs
Strand 4: Geometry and Measurement, Concept 1: Geometric Properties	
PO 1. Recognize the relationship between central angles and intercepted arcs; identify arcs and chords of a circle.	Circles
PO 2. Analyze and determine relationships between angles created by parallel lines cut by a transversal.	Angles made with parallel lines
PO 3. Draw and classify 3-dimensional figures with appropriate labels showing specified attributes of parallelism, congruence, perpendicularity, and symmetry.	Solid shapes Congruence Rotational symmetry

PO 4. Describe the relationship between the number of sides in a regular polygon and the sum of its interior angles.	The sum of interior and exterior angles
PO 5. Identify corresponding parts of congruent figures.	Congruence
Strand 4: Geometry and Measurement, Concept 2: Transformation of Shapes	
PO 1. Model the result of a double transformation (translations or reflections) of a 2-dimensional figure on a coordinate plane using all four quadrants.	Translation Reflection Combining transformations
Strand 4: Geometry and Measurement, Concept 4: Measurement	
PO 1. Solve problems involving the circumference and area of a circle by calculating and estimating.	Circumference of a circle Area of a circle
PO 2. Identify polygons having the same perimeter or area.	Perimeter Area
PO 3. Calculate the area and perimeter of composite 2-dimensional figures.	Area Perimeter Area of irregular shapes
PO 4. Determine actual lengths based on scale drawings or maps.	Scale drawings
PO 5. Create a net to calculate the surface area of a given solid.	Surface area Constructing nets
PO 6. Identify the appropriate unit of measure to compute the volume of an object and justify reasoning.	-
PO 7. Measure to the appropriate degree of accuracy and justify reasoning.	Reading scales Rounding
Grade 8	
Strand 1: Number and Operations, Concept 1: Number Sense	
PO 1. Compare and order real numbers including very large and small integers, and decimals and fractions close to zero.	Ordering decimals Ordering fractions Scientific notation
PO 2. Classify real numbers as rational or irrational.	Rational and irrational numbers
PO 3. Model the relationship between the subsets of the real number system.	-
PO 4. Model and solve problems involving absolute value.	Absolute value

Strand 1: Number and Operations, Concept 2: Numerical Operations	
	Multiples and factors Divisibility Prime numbers Ratio and rate
PO 1. Solve problems with factors, multiples, divisibility or remainders, prime numbers, and composite numbers.	
PO 2. Describe the effect of multiplying and dividing a rational number by •a number less than zero, •a number between zero and one, •one, and •a number greater than one.	Multiplying by numbers between 0 and 1 Multiplying and dividing by 0.1 and 0.01 Multiplying and dividing integers Properties of numbers Multiplying fractions
	Percentage change Calculating percentages mentally Calculating percentages on paper Calculating percentages with a calculator Percentages and inverse operations
PO 3. Solve problems involving percent increase, percent decrease, and simple interest rates.	
PO 4. Convert standard notation to scientific notation and vice versa (include positive and negative exponents).	Scientific notation
	Order of operations and PEMDAS Absolute value Powers Square roots Cubes and cube roots
PO 5. Simplify numerical expressions using the order of operations that include grouping symbols, square roots, cube roots, absolute values, and positive exponents.	
Strand 1: Number and Operations, Concept 3: Estimation	
	Rounding Estimation and approximation Estimating measurements
PO 1. Make estimates appropriate to a given situation.	
	Square roots Estimation and approximation
PO 2. Estimate the location of rational and common irrational numbers on a number line.	

Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 1: Data Analysis (Statistics)	
PO 1. Solve problems by selecting, constructing, interpreting, and calculating with displays of data, including box and whisker plots and scatterplots.	Appropriate graphs Scatter plots Calculating statistics Quartiles and box plots Finding the mode Finding the median Calculating the mean Finding the range Interquartile range Bar graphs Line graphs Circle graphs Histograms
PO 2. Make inferences by comparing the same summary statistic for two or more data sets.	Comparing data Quartiles and box plots Interquartile range
PO 3. Describe how summary statistics relate to the shape of the distribution.	Calculating statistics Comparing data Quartiles and box plots
PO 4. Determine whether information is represented effectively and appropriately given a graph or a set of data by identifying sources of bias and compare and contrast the effectiveness of different representations of data.	Misleading graphs
PO 5. Evaluate the design of an experiment.	Population and sampling Collecting data
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 2: Probability	
PO 1. Determine theoretical and experimental conditional probabilities in compound probability experiments.	-
PO 2. Interpret probabilities within a given context and compare the outcome of an experiment to predictions made prior to performing the experiment.	Experimental probability
PO 3. Use all possible outcomes (sample space) to determine the probability of dependent and independent events.	Probability diagrams

Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 3: Systematic Listing and Counting	
PO 1. Represent, analyze, and solve counting problems with or without ordering and repetitions.	Probability diagrams
PO 2. Solve counting problems and represent counting principles algebraically including factorial notation.	-
Strand 2: Data Analysis, Probability, and Discrete Mathematics, Concept 4: Vertex-Edge Graphs	
PO 1. Use directed graphs to solve problems.	-
Strand 3: Patterns, Algebra, and Functions, Concept 1: Patterns	
PO 1. Recognize, describe, create, and analyze numerical and geometric sequences using tables, graphs, words, or symbols; make conjectures about these sequences.	Introducing sequences Sequences from geometrical patterns Describing and continuing sequences Generating sequences from flow charts Generating sequences and rules Finding the nth term Sequences from practical contexts

Strand 3: Patterns, Algebra, and Functions, Concept 2: Functions and Relationships	
PO 1. Sketch and interpret a graph that models a given context; describe a context that is modeled by a given graph.	Interpreting graphs Distance-time graphs Conversion graphs
PO 2. Determine if a relationship represented by a graph or table is a function.	Function notation and relations
PO 3. Write the rule for a simple function using algebraic notation.	Function machines Mapping functions
PO 4. Identify functions as linear or nonlinear and contrast distinguishing properties of functions using equations, graphs, or tables.	Graphs of functions The equation of a straight line Graphs of nonlinear functions Exploring nonlinear graphs
PO 5. Demonstrate that proportional relationships are linear using equations, graphs, or tables.	Direct variations Exploring nonlinear graphs
Strand 3: Patterns, Algebra, and Functions, Concept 3: Algebraic Representations	
PO 1. Write or identify algebraic expressions, equations, or inequalities that represent a situation.	Solving linear inequalities Writing expressions Introducing formulas
PO 2. Evaluate an expression containing variables by substituting rational numbers for the variables.	Substitution The equation of a straight line
PO 3. Analyze situations, simplify, and solve problems involving linear equations and inequalities using the properties of the real number system.	Properties of numbers Solving simple equations Solving linear inequalities
PO 4. Translate between different representations of linear equations using symbols, graphs, tables, or written descriptions.	Graphs of functions Mapping functions The equation of a straight line
PO 5. Graph an inequality on a number line.	Inequalities on a number line
Strand 3: Patterns, Algebra, and Functions, Concept 4: Analysis of Change	
PO 1. Interpret the relationship between a linear equation and its graph, identifying and computing slope and intercepts.	The equation of a straight line
PO 2. Solve problems involving simple rates.	-
Strand 4: Geometry and Measurement, Concept 1: Geometric Properties	
PO 1. Identify the attributes of circles: radius, diameter, chords, tangents, secants, inscribed angles, central angles, intercepted arcs, circumference, and area.	Circles Circumference of a circle Area of a circle
PO 2. Predict results of combining, subdividing, and changing shapes of plane figures and solids.	Cross sections Tessellations

PO 3. Use proportional reasoning to determine congruence and similarity of triangles.	Congruence Finding missing lengths
PO 4. Use the Pythagorean Theorem to solve problems.	Pythagorean Theorem Identifying right triangles Calculating sides of right triangles Pythagorean triples

Strand 4: Geometry and Measurement, Concept 2: Transformation of Shapes	
PO 1. Model the result of rotations in multiples of 45 degrees of a 2-dimensional figure about the origin.	Rotation
PO 2. Describe the transformations that create a given tessellation.	Tessellations Combining transformations
PO 3. Identify lines of symmetry in plane figures or classify types of symmetries of 2-dimensional figures.	Reflection symmetry Rotational symmetry
Strand 4: Geometry and Measurement, Concept 3: Coordinate Geometry	
PO 1. Make and test a conjecture about how to find the midpoint between any two points in the coordinate plane.	Finding the midpoint of a line segment
PO 2. Use the Pythagorean Theorem to find the distance between two points in the coordinate plane.	-
Strand 4: Geometry and Measurement, Concept 4: Measurement	
PO 1. Solve problems involving conversions within the same measurement system.	Converting metric units Customary unit conversions
PO 2. Solve geometric problems using ratios and proportions.	Finding missing lengths
PO 3. Calculate the surface area and volume of rectangular prisms, right triangular prisms, and cylinders.	Surface area Volume Cylinders, cones and spheres Formulas for shapes